



DBO NOV 2023 VRAESTEL 1 MEMO'S

ALGEBRA & VERGELYKINGS & ONGELYKHEDDE [24]

1.1.1 $x^2 + x - 12 = 0$

$$\therefore (x+4)(x-3) = 0$$

$$\therefore x+4 = 0 \quad \text{of} \quad x-3 = 0$$

$$\therefore x = -4 \leftarrow \quad \therefore x = 3 \leftarrow$$

1.1.2 $3x^2 - 2x = 6$

$$\therefore 3x^2 - 2x - 6 = 0$$

$$\therefore x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(3)(-6)}}{2(3)} \quad \dots \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{2 \pm \sqrt{4 + 72}}{6}$$

$$\approx 1,79 \quad \text{of} \quad -1,12 \leftarrow$$



1.1.3 $\sqrt{2x+1} = x-1$

$$\therefore (\sqrt{2x+1})^2 = (x-1)^2$$

$$\therefore 2x+1 = x^2 - 2x + 1$$

$$\therefore 0 = x^2 - 4x$$

$$\therefore x(x-4) = 0$$

$$\therefore x = 0 \quad \text{of} \quad 4$$

Slegs $x = 4 \leftarrow \quad \dots \quad \text{Vir } x = 0$
 $\sqrt{} \text{ is neg}$

1.1.4 $x^2 - 3 > 2x$

$$\therefore x^2 - 2x - 3 > 0$$

$$\therefore (x-3)(x+1) > 0$$

$$\therefore x < -1 \quad \text{of} \quad x > 3 \leftarrow$$



1.2 $x+2 = 2y$
 $\therefore x = 2y-2 \quad \dots \quad ①$

$$\frac{1}{x} + \frac{1}{y} = 1$$

$$(x \neq 0) \quad \therefore y+x = xy \quad \dots \quad ②$$

① in ②: $\therefore y + (2y-2) = y(2y-2)$
 $\therefore 3y-2 = 2y^2-2y$
 $\therefore 0 = 2y^2-5y+2$
 $\therefore (2y-1)(y-2) = 0$
 $\therefore y = \frac{1}{2} \quad \text{of} \quad y = 2$

Vir $y = \frac{1}{2}$: $x = 2\left(\frac{1}{2}\right) - 2 = -1$

& Vir $y = 2$: $x = 2(2) - 2 = 2$

∴ Oplossing: $\left(-1; \frac{1}{2}\right) \quad \text{of} \quad (2; 2) \leftarrow$

OF:

$$x+2 = 2y$$

$$\therefore x = 2y-2 \quad \dots \quad ①$$

$$\frac{1}{x} + \frac{1}{y} = 1 \quad \dots \quad ②$$

① in ②: $\therefore \frac{1}{2y-2} + \frac{1}{y} = 1 \quad \times y(2y-2)$
 $\therefore y + 2y - 2 = y(2y-2)$
 $\therefore y + 2y - 2 = 2y^2 - 2y$
 $\therefore 2y^2 - 5y + 2 = 0$
 $\therefore (2y-1)(y-2) = 0$
 $\therefore y = \frac{1}{2} \quad \text{of} \quad y = 2$
 $\therefore x = -1 \quad \text{of} \quad x = 2$
 $\therefore \left(-1; \frac{1}{2}\right) \quad \text{of} \quad (2; 2) \leftarrow$

1.3 $2^{m+1} + 2^m = 3^{n+2} - 3^n$
 $\therefore 2^m \cdot 2 + 2^m = 3^n \cdot 3^2 - 3^n$
 $\therefore 2^m(2+1) = 3^n(3^2-1)$
 $\therefore 3 \cdot 2^m = 8 \cdot 3^n$
 $(\div 3 \cdot 8) \quad \frac{2^m}{8} = \frac{3^n}{3}$
 $\therefore \frac{2^m}{2^3} = \frac{3^n}{3}$
 $\therefore 2^{m-3} = 3^{n-1}$

slegs moontlik indien $m-3 = 0$ en $n-1 = 0$
 $\therefore m = 3 \quad \therefore n = 1$

$$\therefore m+n = 4 \leftarrow$$

OF: $2^m(2+1) = 3^n(3^2-1)$

$$\therefore 2^m \cdot 3 = 3^n \cdot 8$$

$$\frac{2^m}{3^n} = \frac{8}{3}$$

$$\therefore \frac{2^m}{3^n} = \frac{2^3}{3}$$

$$\therefore m = 3 \quad \text{en} \quad n = 1$$

$$\therefore m+n = 4 \leftarrow$$



PATRONE & RYE [26]

2.1 **R.R.**: $7 + 12 + 17 + \dots$

2.1.1 $a = 7$; $d = 5$; $T_{91}?$; $n = 91$

$$T_n = a + (n - 1)d$$

$$\therefore T_{91} = 7 + (91 - 1)(5) \\ = 457 \leftarrow$$

OF: Algemene term, $T_n = an + b$
waar $a = 5$ en $b = 2$
 $\therefore T_{91} = 5(91) + 2$
 $= 457 \leftarrow$

2.1.2 $S_n = \frac{n}{2}(a + T_n)$

$$\therefore S_{91} = \frac{91}{2}(7 + T_{91}) \\ = \frac{91}{2}(7 + 457) \\ = 21\ 112 \leftarrow$$



OF: $S_n = \frac{n}{2}[2a + (n - 1)d]$
 $\therefore S_{91} = \frac{91}{2}[2(7) + (91 - 1)(5)]$
 $= 21\ 112 \leftarrow$

2.1.3 $n?$; $T_n = 517$

$$T_n = a + (n - 1)d \Rightarrow 517 = 7 + (n - 1)(5) \\ \therefore 517 = 7 + 5n - 5 \\ \therefore 515 = 5n \\ \therefore n = 103 \leftarrow$$

OF: $T_n = an + b$
 $\therefore 517 = 5n + 2$
 $\therefore 515 = 5n$
 $\therefore n = 103 \leftarrow$

2.2.1 Algemene term: $T_n = an^2 + bn + c$

$$T_1 = 3 ; T_2 - T_1 = 9 \text{ en } T_3 - T_2 = 21$$

\therefore Die patroon:

3	12	33	66	111
9	21	33	45	
12	12	12	12	

1^{ste} verskille:
2^{de} verskille:

$$T_5 = 66 + 45 = 111 \leftarrow$$

2.2.2 $T_1 = a + b + c = 3$

$$2a = 12 \quad \dots \text{Algemene 2^{de} verskil}$$

$$\therefore a = 6$$

$$\& 3a + b = 9 \quad \dots \text{Die eerste 1^{ste} verskil}$$

$$\therefore 18 + b = 9$$

$$\therefore b = -9$$

$$\therefore 6 + (-9) + c = 3$$

$$\therefore c = 6$$

$$\therefore T_n = 6n^2 - 9n + 6 \leftarrow$$

2.2.3 $\frac{dT_n}{dn} = 12n - 9$

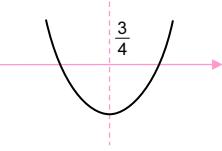
$$\text{As } n > \frac{3}{4} \quad 12n - 9 > 0$$

Aangesien $n \in \mathbb{N}$ sal die afgeleide altyd positief wees

$\therefore T_n$ is altyd stygend vir alle $n \in \mathbb{N}$ \leftarrow

OF: $T_n = 6n^2 - 9n + 6$

$$\text{A van S: } n = -\frac{-9}{2(6)} \\ = \frac{3}{4}$$



$\therefore T_n$ is altyd stygend vir alle $n \in \mathbb{N}$ \leftarrow

OF:

$$\begin{aligned} T_{n+1} - T_n &= 6(n+1)^2 - 9(n+1) + 6 - (6n^2 - 9n + 6) \\ &= 6(n^2 + 2n + 1) - 9n - 9 + 6 - 6n^2 + 9n - 6 \\ &= 6n^2 + 12n + 6 - 9 - 6n^2 \\ &= 12n - 3 \end{aligned}$$

Aangesien $n \geq 1$ en 'n heelgetal is
... aangesien $n = \text{die aantal terme}$

het $12n - 3$ 'n minimum waarde van $12(1) - 3 = 9$, wat positief is

\therefore Die verskil tussen opeenvolgende terme T_n en T_{n+1} sal altyd positief wees.

\therefore Die patroon is stygend vir alle $n \in \mathbb{N}$ \leftarrow



3.1 **M.R.:** $3 + 6 + 12 + \dots$ tot n terme

3.1.1 $a = 3$; $r = 2$

$$T_n = ar^{n-1} \Rightarrow T_n = 3 \cdot 2^{n-1} \blacktriangleleft$$

$$3.1.2 \sum_{p=1}^k \frac{3}{2}(2)^p = 98\ 301 \dots \text{d.w.s. } S_k = 98\ 301$$

$$\begin{aligned} LK &= \frac{3}{2}(2)^1 + \frac{3}{2}(2)^2 + \frac{3}{2}(2)^3 + \dots + \frac{3}{2}(2)^k \\ &= 3 + 6 + 12 + \dots + \frac{3}{2}(2)^k \end{aligned}$$

Som, S_n , van 'n M.R. met $a = 3$; $r = 2$; $n = k$

$$S_n = \frac{a(r^n - 1)}{r - 1}$$

$$\begin{aligned} S_k &= \frac{3(2^k - 1)}{2 - 1} \\ &= 3(2^k - 1) \end{aligned}$$

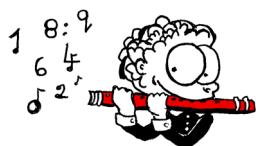
$$\therefore 3(2^k - 1) = 98\ 301$$

$$\therefore 2^k - 1 = 32\ 767$$

$$\therefore 2^k = 32\ 768$$

$$\therefore k = \log_2 32\ 768 \dots \text{OF, deur inspeksie}$$

$$\therefore k = 15 \blacktriangleleft$$



3.2

Rekenkundige Ry

1ste term: $T_1 = x$

$d = 3$

$$S_n = \frac{n}{2}[2a + (n-1)d]$$

$$\begin{aligned} S_{22} &= \frac{22}{2}[2x + (22-1)(3)] \\ &= 11(2x + 63) \\ &= 22x + 693 \end{aligned}$$

Meetkundige Ry

$T_1 = x$

$$r = \frac{1}{3}$$

$$S_\infty = \frac{a}{1-r}$$

$$\begin{aligned} &= \frac{x}{1 - \frac{1}{3}} \\ &= \frac{3x}{3 - 1} \\ &= \frac{3x}{2} \end{aligned}$$

NOTAS

S_{22} van die R.R. = S_∞ van die M.R. + 734

$$\therefore 22x + 693 = \frac{3x}{2} + 734$$

$$(\times 2) \therefore 44x + 1\ 386 = 3x + 1\ 468$$

$$\therefore 41x = 82$$

$$\therefore x = 2$$

d.w.s. $T_1 = 2 \blacktriangleleft$



FUNKSIES & GRAFIEKE [32]

4.1 $y = -4 \blacktriangleleft$

4.2 By B, $y = 0$

$$\therefore 2^x - 4 = 0$$

$$\therefore 2^x = 4$$

$$\therefore x = 2$$

$$\therefore B(2; 0) \blacktriangleleft$$

4.3 y-afsnit van f:

$$f(0) = 2^0 - 4 = 1 - 4 = -3$$

$$\therefore A(0; -3)$$

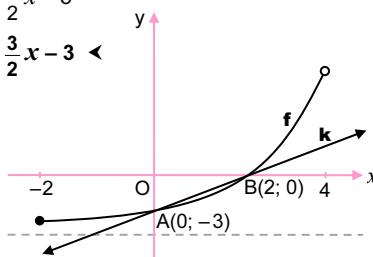
Y-afsnit van k, c = -3

Gradiënt, m = $\frac{3}{2}$... deur inspeksie

$$\text{(of: } m_{AB} = \frac{0 - (-3)}{2 - 0} = \frac{3}{2} \text{)}$$

$$\therefore \text{Verg. van k: } y = \frac{3}{2}x - 3$$

$$\text{d.w.s. } k(x) = \frac{3}{2}x - 3 \blacktriangleleft$$



4.4 Die vertikale afstand = $k(x) - f(x)$

$$= k(1) - f(1)$$

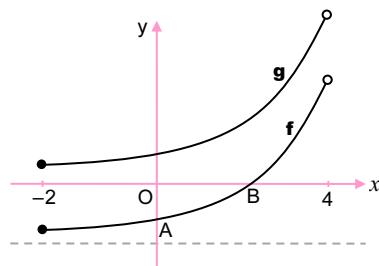
$$= -\frac{3}{2} - (-2) \dots$$

$$k(1) = \frac{3}{2}(1) - 3 \quad \&$$

$$f(1) = 2^1 - 4$$

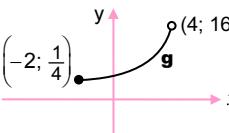
$$= \frac{1}{2} \text{ eenheid} \blacktriangleleft$$

4.5 $g(x) = 2^x - 4 + 4$
 $\therefore g(x) = 2^x \blacktriangleleft \text{ vir } x \in [-2; 4)$



4.6 Die definisieversameling van g^{-1} = die waardeversameling van g
 waardeversameling van g:

$$\frac{1}{4} \leq y < 16$$



$$\therefore \text{definisieversameling van } g^{-1}: \frac{1}{4} \leq x < 16 \blacktriangleleft$$

4.7 $y = \log_2 x \text{ vir } x \in \left[\frac{1}{4}; 16\right] \blacktriangleleft$

NOTAS



5.1 Draaipunt van f : $B(1; 8)$ ↵

5.2 By C , $x = 0$

$$\& f(0) = -\frac{1}{2}(0-1)^2 + 8 = 7\frac{1}{2}$$

$$\therefore C\left(0; 7\frac{1}{2}\right) \hookrightarrow$$

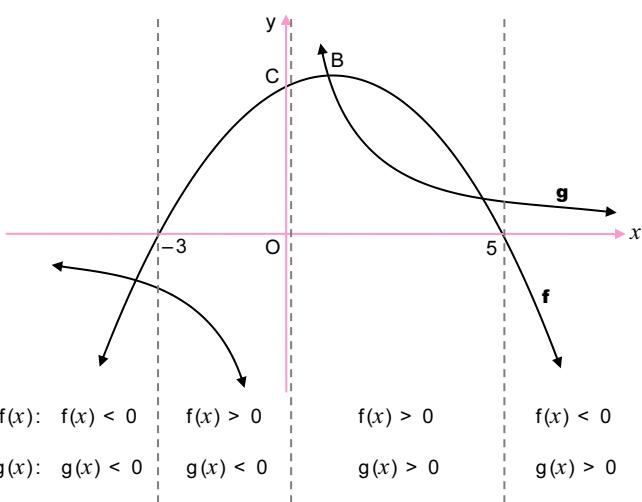
5.3 $B(1; 8)$ 'n punt op g

$$\Rightarrow g(1) = \frac{d}{1} = 8 \quad \dots g(x) = \frac{d}{x}$$

$$\therefore d = 8 \hookrightarrow$$

5.4 $y \in \mathbb{R}; y \neq 0 \hookrightarrow$

5.5 $-3 \leq x < 0$ of $x \geq 5 \hookrightarrow$



5.6 By enige snypunt(e):

$$h(x) = g(x)$$

$$\therefore -2x + k = \frac{8}{x}$$

$$(x \cdot x) \therefore -2x^2 + kx = 8$$

$$\times (-1) \therefore 2x^2 - kx + 8 = 0$$

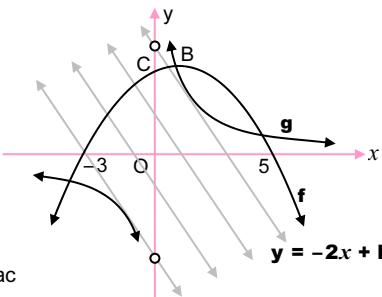
$$\Delta = (-k)^2 - 4(2)(8) \quad \Delta = b^2 - 4ac \\ = k^2 - 64$$

Daar sal geen snypunte wees as $\Delta < 0$

$$k^2 - 64 < 0$$

$$\therefore (k+8)(k-8) < 0$$

$$\therefore -8 < k < 8 \hookrightarrow$$



5.7 $g'(x) = -\frac{8}{x^2}$

$$\therefore -\frac{8}{x^2} = -2$$

$$\therefore x^2 = 4$$

$$\therefore x = \pm 2$$

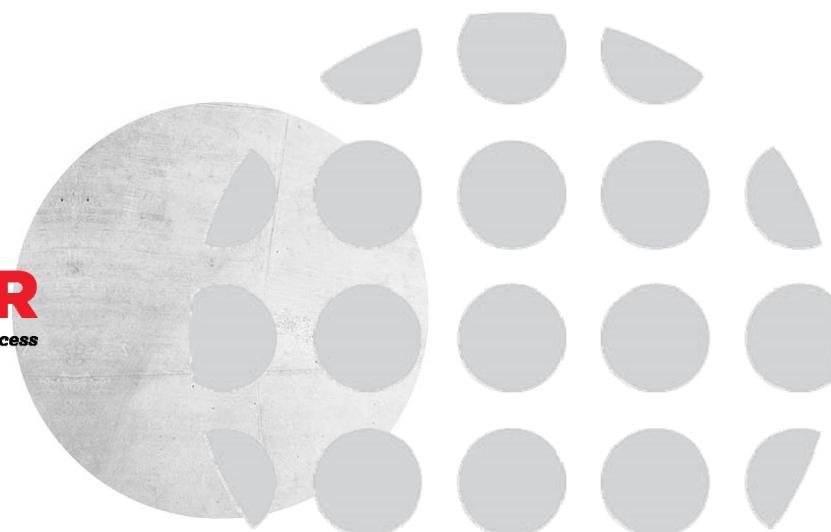
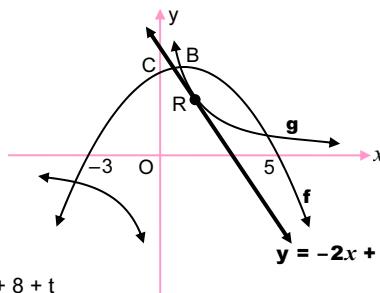
$$\therefore R(2; 4)$$

$$y = -\frac{1}{2}(x-1)^2 + 8+t$$

$$\therefore 4 = -\frac{1}{2}(2-1)^2 + 8+t$$

$$\therefore 4 = -\frac{1}{2} + 8+t$$

$$\therefore t = -3\frac{1}{2} \hookrightarrow$$



FINANSIES, GROEI & VERVAL [16]

6.1 $P = R18\ 500 ; i = \frac{r}{12} \% ; n = 6 ; A = 19\ 319,48$

6.1.1 $A = P(1 + r)^n \Rightarrow 19\ 319,48 = 18\ 500 \left(1 + \frac{i}{12}\right)^6$

$$\therefore \left(1 + \frac{i}{12}\right)^6 = \frac{19\ 319,48}{18\ 500} = 1,04429\dots$$

$$\therefore 1 + \frac{i}{12} = \sqrt[6]{1,04429\dots} = 1,00725\dots$$

$$\therefore \frac{i}{12} = 0,00725$$

$$\therefore i \approx 0,087$$

$$\therefore r \approx 8,70\% \blacktriangleleft$$



6.1.2 $1 + i_{\text{eff}} = \left(1 + \frac{i_{\text{nom}}}{m}\right)^m$

$$\therefore 1 + i_{\text{eff}} = \left(1 + \frac{0,087}{12}\right)^{12}$$

$$\therefore 1 + i_{\text{eff}} = 1,09055\dots$$

$$\therefore i_{\text{eff}} = 0,09055\dots \approx 9,06\% \blacktriangleleft$$

6.2.1 Die waarde van die skootrekenaar daal tot R0:

$$P = R10\ 000 ; n? ; i = 0,2 ; A = R0$$

$$A = P(1 - in) \Rightarrow 0 = 10\ 000(1 - 0,2n)$$

$$\therefore 0 = 1 - 0,2n$$

$$\therefore 0,2n = 1$$

$$\therefore n = \frac{1}{0,2}$$

$$\therefore n = 5 \text{ jaar} \blacktriangleleft$$



6.2.2 Nuwe skootrekenaar:

$$F_v = R20\ 000 ; n = 60 ; i = \frac{8,7\%}{12} = \frac{0,087}{12}$$

$$F_v = \frac{x[(1+i)^n - 1]}{i} \Rightarrow 20\ 000 = \frac{x\left[\left(1 + \frac{0,087}{12}\right)^{60} - 1\right]}{\frac{0,087}{12}}$$

$$\therefore x = 267,2611\dots$$

$\therefore x = R267,27 \blacktriangleleft \dots R267,26 sal 'n waarde net minder as R20\ 000 gee$

6.3 $P_v = R1\ 600\ 000 ; i = \frac{11,2\%}{12} ; x = 20\ 000 ; n?$

$$P_v = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$1\ 600\ 000 = \frac{20\ 000 \left[1 - \left(1 + \frac{11,2\%}{12}\right)^{-n}\right]}{\frac{11,2\%}{12}}$$

$$\therefore 80 = \frac{\left[1 - \left(1 + \frac{0,112}{12}\right)^{-n}\right]}{\frac{0,112}{12}}$$

$$\left(\times \frac{0,112}{12}\right) \quad \therefore \frac{56}{75} = 1 - \left(1 + \frac{0,112}{12}\right)^{-n}$$

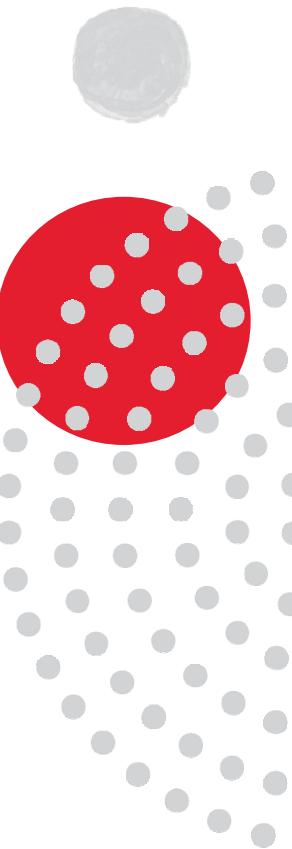
$$\therefore \left(1 + \frac{0,112}{12}\right)^{-n} = 1 - \frac{56}{75}$$

$$\therefore -n = \log\left(1 + \frac{0,112}{12}\right)^{\frac{19}{75}}$$

$$= -147,79\dots$$

$$\therefore n = 147,79\dots$$

\therefore Hy sal 147 ontrekkings van R20\ 000 kan maak \blacktriangleleft



DIFFERENSIAALREKENE [37]

$$7.1 \quad f(x) = -4x^2$$

$$\begin{aligned} \therefore f(x+h) &= -4(x+h)^2 \\ &= -4(x^2 + 2xh + h^2) \\ &= -4x^2 - 8xh - 4h^2 \end{aligned}$$

$$\therefore f(x+h) - f(x) = -8xh - 4h^2$$

$$\therefore \frac{f(x+h) - f(x)}{h} = -8x - 4h$$

$$\begin{aligned} \therefore f'(x) &= \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \\ \text{def van 'n afgeleide} &= \lim_{h \rightarrow 0} (-8x - 4h) \\ &= -8x \quad \blacktriangleleft \end{aligned}$$

$$\left. \begin{aligned} \text{OF: } f'(x) &= \lim_{h \rightarrow 0} \frac{-4(x+h)^2 - (-4x^2)}{h} \\ &= \lim_{h \rightarrow 0} \frac{-4x^2 - 8xh - 4h^2 + 4x^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{-8xh - 4h^2}{h} \\ &= \lim_{h \rightarrow 0} (-8x - 4h) \\ &= -8x \end{aligned} \right\}$$

$$7.2.1 \quad f(x) = 2x^3 - 3x$$

$$\therefore f'(x) = 6x^2 - 3 \quad \blacktriangleleft$$

$$7.2.2 \quad D_x(7 \cdot x^{\frac{2}{3}} + 2x^{-5})$$

$$\begin{aligned} &= 7 \cdot \frac{2}{3} x^{-\frac{1}{3}} + 2 \cdot -5x^{-6} \\ &= \frac{14}{3} \cdot x^{-\frac{1}{3}} - 10x^{-6} \quad \blacktriangleleft \end{aligned}$$

$$\left. \begin{aligned} &= \frac{14}{3x^{\frac{1}{3}}} - \frac{10}{x^6} \quad \blacktriangleleft \\ &= \frac{14}{3\sqrt[3]{x}} - \frac{10}{x^6} \quad \blacktriangleleft \end{aligned} \right\}$$



7.3

Die raaklyn aan 'n grafiek:

Die gradiënt van die raaklyn aan 'n grafiek f is die afgeleide, $f'(x)$

$$f(x) = -2x^3 + 8x$$

$$\therefore \text{Die gradiënt van die raaklyn} = f'(x) = -6x^2 + 8$$

$$f'(x) > 0 \Rightarrow -6x^2 + 8 > 0$$

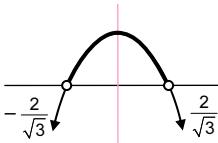
Die grafiek van $y = f'(x)$:

Die wortels: $-6x^2 + 8 = 0$

$$\therefore 6x^2 = 8$$

$$\therefore x^2 = \frac{4}{3}$$

$$\therefore x = \pm \frac{2}{\sqrt{3}}$$



$$\therefore -\frac{2}{\sqrt{3}} < x < \frac{2}{\sqrt{3}} \quad \blacktriangleleft$$

[of $-1,15 < x < 1,15 \quad \blacktriangleleft$]



NOTAS



8.1 $f(x) = -x^3 + 6x^2 - 9x + 4 = (x - 1)^2(-x + 4)$

By die draapunte, $f'(x) = 0$

$$\therefore f'(x) = -3x^2 + 12x - 9 = 0$$

$$\div (-3): \therefore x^2 - 4x + 3 = 0$$

$$\therefore (x - 1)(x - 3) = 0$$

$$\therefore x = 1 \text{ of } 3$$

$$f(1) = (1 - 1)^2(-1 + 4) = 0$$

$$\& f(3) = (3 - 1)^2(-3 + 4) = 4$$

\therefore Draapunte is $(1; 0)$ en $(3; 4)$ ↵

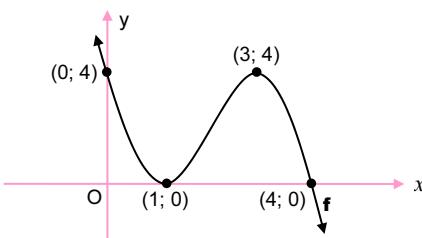
8.2 **Y-afsnit:** $f(0) = 4$

$$(x = 0) \therefore (0; 4)$$

X-afsnitte: $(x - 1)^2(-x + 4) = 0$

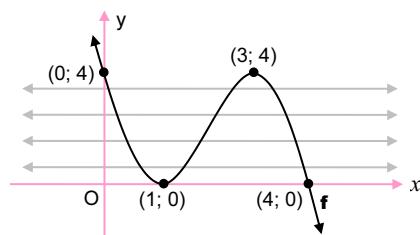
$$(y = 0) \therefore x = 1 \text{ ('twee keer': dit is ook 'n draapunt)} \\ \text{of } x = 4$$

$$\therefore (1; 0) \text{ en } (4; 0)$$



8.3 $0 < k < 4$ ↵

$y = k$ kan (die vgl van) enige van hierdie grys lyne wees.
Hulle sny almal vir f by 3 duidelike punte.



8.4 By die buigpunt: $f''(x) = 0$

$$\therefore f''(x) = -6x + 12 = 0$$

$$\therefore -6x = -12$$

$$\therefore x = 2$$

$$f(2) = 2$$

\therefore Die buigpunt is $(2; 2)$ ↵

Die gradiënt van die raaklyn aan f ,

$$a = f'(2) = -3(2)^2 + 12(2) - 9$$

$$= -12 + 24 - 9$$

$$= 3$$

Stel $a = 3$ en $(2; 2)$ in $y = ax + b$ in:

$$\therefore 2 = (3)(2) + b \quad \text{of } y - y_1 = m(x - x_1)$$

$$\therefore b = -4 \quad \therefore y - 2 = 3(x - 2), \text{ ens.}$$

\therefore Die vergelyking van g : $y = 3x - 4$ ↵



NOTAS

8.5 $\tan \theta = 3 \dots$ die gradiënt van g

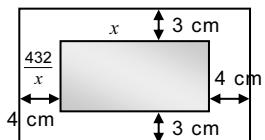
$$\therefore \theta = 71,57^\circ \hookrightarrow$$



9.1 Die oppervlakte van reghoek ABCD:

$$x \times AB = 432 \text{ cm}^2$$

$$\therefore AB = \frac{432}{x} \text{ cm}$$



$$\therefore \text{Die totale oppervlakte} = (x + 8) \left(\frac{432}{x} + 6 \right)$$

$$= 432 + 6x + \frac{3456}{x} + 48$$

$$= \frac{3456}{x} + 6x + 480 \blacktriangleleft$$

9.2 Die totale oppervlakte, $A = 3456x^{-1} + 6x + 480$

$$\text{Vir minimum waarde, } \frac{dA}{dx} = 0$$

$$\therefore -3456x^{-2} + 6 = 0$$

$$\therefore -\frac{3456}{x^2} = -6$$

$$\times(-x^2) \quad \therefore 3456 = 6x^2$$

$$(\div 6) \quad \therefore 576 = x^2$$

$$\therefore x = 24 \text{ cm} \quad \dots x > 0 \blacktriangleleft$$

NOTAS



WAARSKYNLIKHEID [15]

10.1.1 Vir onafhanklike gebeurtenisse, A en B:

$$\begin{aligned} P(A \text{ en } B) &= P(A) \times P(B) \\ &= \frac{1}{3} \times \frac{3}{4} \\ &= \frac{1}{4} \end{aligned}$$

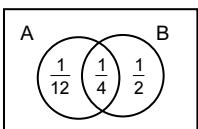
10.1.2 $P(\text{ten minste EEN gebeurtenis vind plaas})$

$$\begin{aligned} &= P(A \text{ of } B) \\ &= P(A) + P(B) - P(A \text{ en } B) \\ &= \frac{1}{3} + \frac{3}{4} - \frac{1}{4} \\ &= \frac{5}{6} \end{aligned}$$

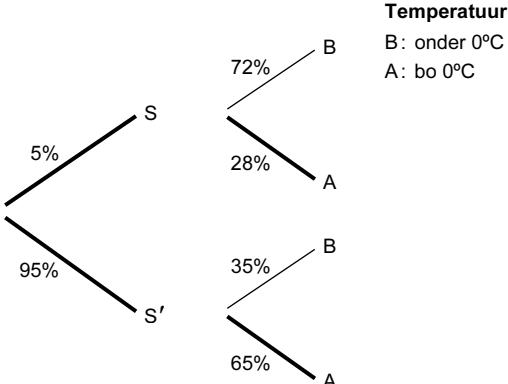


OF: $P(\text{ten minste EEN gebeurtenis vind plaas})$

$$\begin{aligned} &= \frac{1}{12} + \frac{1}{4} + \frac{1}{2} \\ &= \frac{5}{6} \end{aligned}$$



10.2.1



$$\begin{aligned} 10.2.2 \quad P(A) &= P(S \text{ en } A) + P(S' \text{ en } A) \\ &= 5\% \times 28\% + 95\% \times 65\% \\ &= 1,4\% + 61,75\% \\ &= 63,15\% \end{aligned}$$

10.3.1 Aantal maniere: 10 9 8 7 6 5 4 3 2 1
 $\therefore 10! = 3\ 628\ 800 \leftarrow$

10.3.2 Die jongste leerders met 5 leerders tussenin.

2 8 7 6 5 4 1

Dink aan die twee jongste leerders en 5 leerders tussenin as een eenheid. Rangskik dus 4 'groepes', d.w.s. 4!

$$\begin{aligned} \text{aantal maniere} &= 4! \times (2 \times 8 \times 7 \times 6 \times 5 \times 4 \times 1) \\ &= 322\ 560 \end{aligned}$$

$$\therefore \text{WAARSKYNLIKHEID} = \frac{322\ 560}{3\ 628\ 800} \dots P(E) = \frac{n(E)}{n(S)}$$

$$= \frac{4}{45} \leftarrow$$

OF:

$$\begin{aligned} &\underline{2} \times \underline{8} \times \underline{7} \times \underline{6} \times \underline{5} \times \underline{4} \times \underline{1} \times \underline{3} \times \underline{2} \times \underline{1} \\ &\underline{8} \times \underline{2} \times \underline{7} \times \underline{6} \times \underline{5} \times \underline{4} \times \underline{3} \times \underline{1} \times \underline{2} \times \underline{1} \\ &\underline{8} \times \underline{7} \times \underline{2} \times \underline{6} \times \underline{5} \times \underline{4} \times \underline{3} \times \underline{2} \times \underline{1} \times \underline{1} \\ &\underline{8} \times \underline{7} \times \underline{6} \times \underline{2} \times \underline{5} \times \underline{4} \times \underline{3} \times \underline{2} \times \underline{1} \times \underline{1} \end{aligned}$$

$$\therefore \text{WAARSKYNLIKHEID} = \frac{4 \times 2 \times 8!}{10!} \dots P(E) = \frac{n(E)}{n(S)}$$

$$= \frac{4}{45} \leftarrow$$

OF:

$$P(\text{enige een van twee jongste leerders}) = \frac{2}{10}$$

$$P(\text{ander jongste leerder}) = \frac{1}{9}$$

Jongste leerders kan in posisies 1 en 7 wees, of 2 en 8, of 3 en 9, of 4 en 10.

$$\therefore \text{WAARSKYNLIKHEID} = \frac{2}{10} \times \frac{1}{9} \times 4$$

$$= \frac{4}{45} \leftarrow$$