

Clearly show ALL calculations, diagrams, graphs, etc. that you have used in determining your answers.

Answers only will NOT necessarily be awarded full marks.

You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.

If necessary, round off answers to **TWO** decimal places, unless stated otherwise.

Diagrams are NOT necessarily drawn to scale.

### **STATISTICS** [20]

#### **QUESTION 1**

Truck drivers travel a certain distance and have a rest before travelling further. A driver kept record of the distance he travelled (in km) on 8 trips and the amount of time he rested (in minutes) before he continued his journey. The information is given in the table below.

| Distance travelled<br>(in km) ( <i>x</i> ) | 180 | 200 | 400 | 600 | 170 | 350 | 270 | 300 |  |
|--|-----|-----|-----|-----|-----|-----|-----|-----|--|
| Amount of rest time<br>(in minutes) (y)    | 20  | 25  | 55  | 120 | 15  | 50  | 40  | 45  |  |

- 1.1 Determine the equation of the least squares regression line for the data. (3)
- 1.2 If a truck driver travelled 550 km, predict the amount of time (in minutes) that he should rest before continuing his journey. (2)
- 1.3 Write down the correlation coefficient for the data.
- 1.4 Interpret your answer to QUESTION 1.3.
- 1.5 At each stop, the truck driver spent money buying food and other refreshments. The amount spent (in rands) is given in the table below.

100 150 130 200 50 180 200 190

- 1.5.1 Calculate the mean amount of money he spent at each shop. (2)
- 1.5.2 Calculate the standard deviation for the data. (1)
- 1.5.3 At how many stops did the driver spend an amount that was less than one standard deviation below the mean? (2) [12]

**QUESTION 2** 

(1)

(1)

At a certain school, the staff committee wanted to determine how many glasses of water the staff members drank during a school day. All teachers present on a specific day were interviewed. The information is shown in the table below.

| NUMBER OF<br>GLASSES OF WATER<br>DRANK PER DAY | NUMBER OF<br>STAFF<br>MEMBERS | CUMULATIVE<br>FREQUENCY |
|--|-------------------------------|-------------------------|
| $0 \le x \le 2$                                | 5                             |                         |
| $2 \le x < 4$                                  | 15                            |                         |
| $4 \le x < 6$                                  | 13                            |                         |
| $6 \le x < 8$                                  | 5                             |                         |
| 8 ≤ <i>x</i> < 10                              | 2                             |                         |

- 2.1 Complete the cumulative frequency column provided in the table above.
- 2.2 How many staff members were interviewed?
- 2.3 How many staff members drank fewer than 6 glasses of water during a school day?
- 2.4 The staff committee observed that k teachers were absent on the day of the interviews. It was found that half of these k teachers drank from 0 to fewer than 2 (that is  $0 \le x < 2$ ) glasses of water per day, while the remainder of them drank from 4 to fewer than 6 (that is  $4 \le x < 6$ ) glasses of water per day. When these k teachers are included in the data, the estimated mean is 4 glasses of water per staff member per day.

How many teachers were absent on the day of the interviews?



# ► ANALYTICAL GEOMETRY [40]

### **QUESTION 3**

(2)

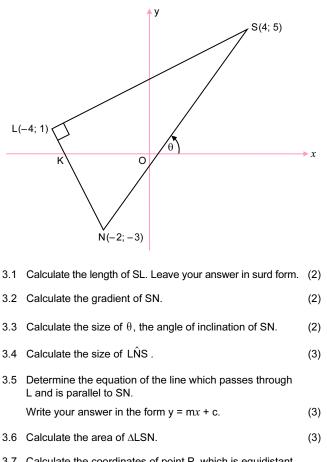
(1)

(1)

(4)

[8]

In the figure, L(-4; 1), S(4; 5) and N(-2; -3) are the vertices of a triangle having  $\hat{SLN} = 90^{\circ}$ . LN intersects the *x*-axis at K.

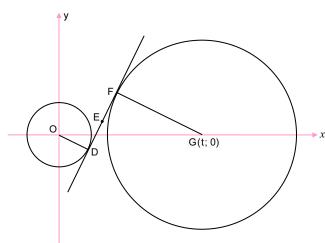


- 3.7 Calculate the coordinates of point P, which is equidistant from L, S and N. (3)
- 3.8 Calculate the size of LPS. (2)

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#### **QUESTION 4**

In the diagram, the circle with centre O has the equation  $x^2 + y^2 = 20$ . G(t; 0) is the centre of the larger circle. A common tangent touches the circles at D and F respectively, such that D(p; -2) lies in the 4<sup>th</sup> quadrant.



- 4.1 Given that D(p; -2) lies on the smaller circle, show that p = 4.
- 4.2 E(6; 2) is the midpoint of DF. Determine the coordinates of F.
- 4.3 Determine the equation of the common tangent, DF, in the form y = mx + c.
- 4.4 Calculate the value of t. Show ALL working.
- 4.5 Determine the equation of the larger circle in the form  $ax^2 + by^2 + cx + dy + e = 0.$
- 4.6 The smaller circle must be translated by k units along the *x*-axis to touch the larger circle internally. Calculate the possible values of k.



# **• TRIGONOMETRY** [50]

# **QUESTION 5**

(2)

(3)

(4)

(3)

(4)

(4)

[20]

5.1 Given:  $\sin \beta = \frac{1}{3}$ , where  $\beta \in (90^{\circ}; 270^{\circ})$ .

Without using a calculator, determine each of the following:

| 5.1.1 | cos β                     | (3) |
|-------|---------------------------|-----|
| 5.1.2 | sin 2β                    | (3) |
| 5.1.3 | $\cos(450^\circ - \beta)$ | (3) |

5.2 Given: 
$$\frac{\cos^4 x + \sin^2 x \cdot \cos^2 x}{1 + \sin x}$$

5.2.1 Prove that 
$$\frac{\cos^4 x + \sin^2 x \cdot \cos^2 x}{1 + \sin x} = 1 - \sin x$$
 (4)

- 5.2.2 For what value(s) of x in the interval  $x \in [0^{\circ}; 360^{\circ}]$ is  $\frac{\cos^4 x + \sin^2 x \cdot \cos^2 x}{1 + \sin x}$  undefined? (2)
- 5.2.3 Write down the minimum value of the function defined by  $y = \frac{\cos^4 x + \sin^2 x \cdot \cos^2 x}{1 + \sin x}$
- 5.3 Given: cos(A B) = cos A cos B + sin A sin B

5.3.1 Use the above identity to deduce that sin(A - B) = sin A cos B - cos A sin B

5.3.2 Hence, or otherwise, determine the general solution of the equation

 $\sin 48^{\circ} \cos x - \cos 48^{\circ} \sin x = \cos 2x$ 

5.4 Simplify  $\frac{\sin 3x + \sin x}{\cos 2x + 1}$  to a single trigonometric ratio.



# **QUESTION** 6

(2)

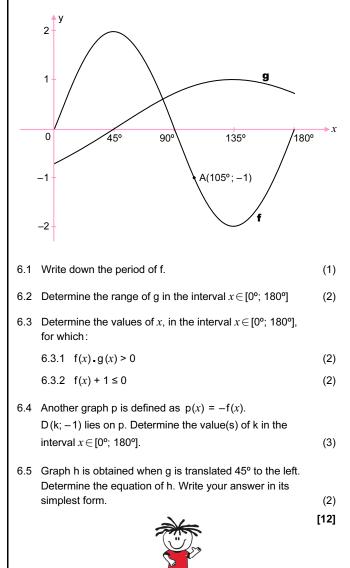
(3)

(5)

(6)

[31]

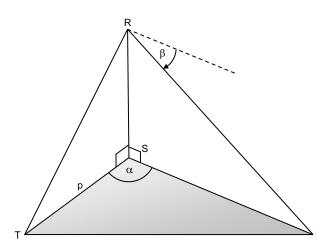
In the diagram, the graphs of  $f(x) = 2 \sin 2x$  and  $g(x) = -\cos(x + 45^{\circ})$  are drawn for the interval  $x \in [0^{\circ}; 180^{\circ}]$ .  $A(105^{\circ}; -1)$  lies on f.



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#### **QUESTION 7**

In the diagram, S, T and K lie in the same horizonal plane. RS is a vertical tower. The angle of depression from R to K is  $\beta$ . TŜK =  $\alpha$ , TS = p metres and the area of  $\Delta$ STK is q m<sup>2</sup>.



- 7.1 Determine the length of SK in terms of p, q and  $\alpha$ .
- 7.2 Show that RS =  $\frac{2q \tan \beta}{p \sin \alpha}$
- 7.3 Calculate the size of  $\alpha$  if  $\alpha < 90^{\circ}$  and RS = 70 m, p = 80 m, q = 2 500 m<sup>2</sup> and  $\beta$  = 42°.



# ► EUCLIDEAN GEOMETRY [40]

#### **QUESTION 8**

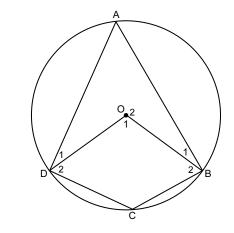
(2)

(2)

(3) [7] 8.1 In the diagram, O is the centre of the circle.

Use the diagram alongside to prove the theorem which states that the angle subtended by a chord at the centre of the circle is equal to twice the angle subtended by the same chord at the circumference, that is, prove that  $T\hat{OP} = 2T\hat{K}P$ .

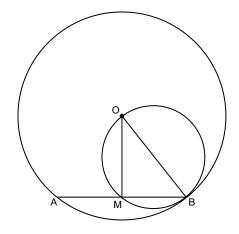
- 8.2 In the diagram, O is the centre of the circle and ABCD is a cyclic quadrilateral. OB and OD are drawn.



If  $\hat{O}_1 = 4x + 100^\circ$  and  $\hat{C} = x + 34^\circ$ , calculate, giving reasons, the size of *x*.



8.3 In the diagram, O is the centre of the larger circle. OB is a diameter of the smaller circle. Chord AB of the larger circle intersects the smaller circle at M and B.

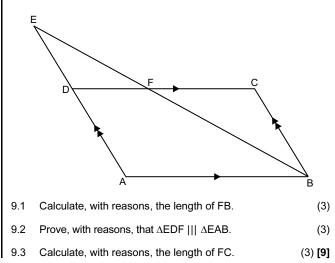


- 8.3.1 Write down the size of OMB. Provide a reason. (2)
- 8.3.2 If AB =  $\sqrt{300}$  units and OM = 5 units, calculate, giving reasons, the length of OB. (4) [16]

#### **QUESTION 9**

(5)

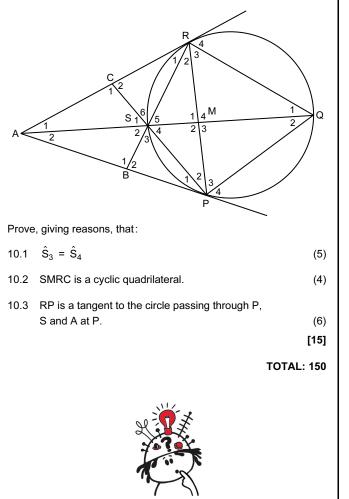
In the diagram, ABCD is a parallelogram with AB = 14 units. AD is produced to E such that AD : DE = 4 : 3. EB intersects DC in F. EB = 21 units.



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### **QUESTION 10**

In the diagram, PQRS is a cyclic quadrilateral such that PQ = PR. The tangents to the circle through P and R meet QS produced at A. RS is produced to meet tangent AP at B. PS is produced to meet tangent AR at C. PR and QS intersect at M.





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