MATHS LITERACY TEACHER SUPPORT WORKSHOP MEASUREMENT - Tips & Tricks

CLASSROOM RESOURCES



Baseline Assessment for Measurement

A school needs to determine how many workers it needs to host a carnival with 15 different rides and an estimated attendance of 3 250 people.

1. Determine how many workers are needed per day. Use the formula:

Workers per day = *number of rides* x 2 + 8

The workers need to wipe down the rides with, on average, 5ℓ of disinfectant per ride.

2. Determine how many bottles of disinfectant will be needed, if they are sold in 12ℓ tins.

Answers



HANDS ON EXPLORATION - PART 1

DIMENSIONS

Dimensions

Choose 2 rectangular containers and 2 cylindrical containers. Using your ruler, determine the following:

RECTANGULAR CONTAINERS

CYLINDRICAL CONTAINERS

1.	Container A : Measure the dimensions in cm: Length: Breadth: Height:	1.	Container A : Measure the dimensions in mm: Radius: Diameter: Height:
2.	Container B : Measure the dimensions in cm: Length: Breadth: Height:	2.	Container B : Measure the dimensions in mm: Radius: Diameter: Height:
3.	Which rectangular container is the deepest and by how much?	3.	Which cylindrical container is the widest and by how much?

HANDS ON EXPLORATION - PART 2

cm

		•	
CO	nve	rsic	ns

Using the same 2 rectangular & 2 cylindrical containers from Part 1, convert:

RECTANGULAR CONTAINERS

4.	 Container A: Convert your measurements from Part 1 from cm to the following: 				
	Length:	cm =	mm		
	Breadth:	cm =	m		
	Height:	cm =	km		

Height:km

CYLINDRICAL CONTAINERS

- - Height:km
- Container B: Convert your measurements from Part 1 from mm to the following: Radius: mm =

Diameter:	mm =m
Height:	mm =km

HANDS ON EXPLORATION PART 3

Costing & Spread Rate Using the same containers from Part 1 & 2, determine the following: **RECTANGULAR CONTAINERS CYLINDRICAL CONTAINERS** 6. Calculate the TSA (excluding the lid) in cm². 6. If you put the smallest container into the larger container, determine the empty space between the two containers A and B in cm³. Formula of a cylindrical container with a closed lid = Volume = length × breadth × height $(2 \times \pi \times radius^2) + (2 \times \pi \times radius \times height);$ where $\pi = 3,142$ 7. If you had to fill the empty space between the two containers with 7. If you had to paint the container (excluding the lid), determine the oil, calculate the total cost of oil if it costs R65 per liter and is sold cost of the paint if the paint is sold for R49,99 per 500 ml bottle only in 2 liter bottles. and the spread rate of the paint is 800 cm²/ ℓ .

IRREGULAR SHAPES & COSTING

DIMENSIONS

CONSOLIDATION - PART 1

Inner vs Outer Dimensions

Aldon is making a circular speed limit sign sticker, which measures 42 cm in diameter. The sticker will then be stuck in the centre of a circular metal backing, with a 6 cm space between the edge of the sticker and the edge of the metal backing, as shown below:

Diameter = 42 cm

Rebecca would like to install a square pool, with a depth of 1,7 m, in her square garden which measures 8 m \times 8 m. She needs to have a 2,5 m paving all around the pool, as shown below:

1. Determine the dimensions of the pool.

Spacing = 6 cm

CONSOLIDATION – PART 2

FORMULAE

CONSOLIDATION PART 3

IRREGULAR SHAPES & COSTING

FORMULAE

Worked Examples - Reverse calculations

A preschooler was told to make a basic figure of a "man" by cutting and pasting a triangle (for the hat), circle (for the face) and rectangle (for the body), as shown alongside: side, = 9 cm side₂ = 6 cm 1. Determine the base of the triangle, given that the perimeter of the triangle is 25 cm. Use the formula: base = ?Perimeter = side, + side, + base ′radius = ? Perimeter = side, + side, + base 25 = 9 + 6 + base... substitute 25 = 15 + base... simplify first! length = ? 25 - 15 = base... opposite operation 10 cm = base... simplify & add units breadth = 8 cm $+ \leftrightarrow -$ Keep variables on the given side!

FORMULAE

Worked Examples - Reverse calculations

variables on the given side!

side₂ = 6 cm

base = ?

side, = 9 cm

Worked Examples - Reverse calculations

A preschooler was told to make a basic figure of a "man" by cutting and pasting a triangle (for the hat), circle (for the face) and rectangle (for the body), as shown alongside:

3. Determine the radius of the man's face, if the area is 78,55 cm². Use the formula:

Exam Practice!

Use the information and picture above to answer the questions that follow

3.2.1	Determine the maximum height (in cm) of the water in the bucket if the outside diameter of the bucket is $31,2$ cm.						
	You	a may use the formula:					
	Volume of a cylinder = $\pi \times (radius)^2 \times height$						
	whe	ere $\pi = 3,142$ and $1 \ell = 1 000 \text{ cm}^3$	(7)				
3.2.2	Buc	kets are placed on the pallet, as shown in the diagram above.					
	(a)	Calculate the unused area (in $\mbox{cm}^2)$ of the rectangular floor of the solid pallet.					
		You may use the formula:					
		Area of a circle = $\pi \times (radius)^2$, where $\pi = 3,142$	(6)				
	(b)	Determine length C, as shown in the diagram above.	(3)				

Answers

FORMULAE

Approaching Irregular Shapes

IRREGULAR SHAPES & COSTING

Spread Rates & Costing

IRREGULAR SHAPES & COSTING

Painting a bedroom with TSA = 147 m^2

Spread rate of paint = $20 \text{ m}^2/\ell$

Paint needed (ℓ) = 147 m² ÷ 20 m²/ ℓ = 7,35 ℓ

Tins come in 2 ℓ @ R199 per tin

Number of tins = 7,35 ℓ ÷ 2 ℓ = 3,675 ≈ 4 tins

∴ Cost m = 4 tins × R199 per tin = R796

Let's Practice!

IRREGULAR SHAPES & COSTING

- 1.7 Calculate the total area of the kennel in m^2 (the shaded area on the drawing).
- 1.8 Calculate the area of the sheet of plywood that will not be used (*the unshaded area on the drawing*).

1.5 Door = rectangle $+\frac{1}{2}$ circle = $(l \times b) + (\frac{1}{2}, \pi r^2)$ = $(0,30 \times 0,25) + (\frac{1}{2} \times 3,142 \times 0,15^2)$ = 0,075 + 0,0353= $0,11 m^2$ 250 mm = 0,25 m300 mm = 0,3 mdiameter $= \frac{0,3}{2}$ = 0,15 m1.6 Area front panel = area back panel - area door = $0,56 - 0,11 = 0,45 m^2$ 1.7 TSA = front + back + side panels = $0,45 + 0,56 + 1,2 = 2,21 m^2$ 1.8 Unshaded area = (total area of plywood - used area)

= (1,2×2,4)-2,21

 $= 2,88 - 2,21 = 0,67 \text{ m}^2$

Conversions

Pop Quiz!

- 1. How many days in a year?
- 2. How many minutes in an hour?

TIME

- 3. How many hours in a day?
- 4. How many seconds in a minute?
- 5. How many months in a year?
- 6. How many days in May?
- 7. How many working days in a week?

Let's Practice – CHALLENGE!

Convert 557 799 seconds to days, hours, minutes and seconds.

Answer

- $557\ 799\ s = 557\ 799 \div 60 = 9\ 296,65\ min$ $\therefore \ 9\ 296,65\ min = 9\ 296,65 \div 60\ s$
 - = 154,9441667 h
- \therefore 154,9441667 h = 154,9441667 \div 24 = 6,456006944 days
- ∴ 6,456006944 days
 - = 6 days + 0,456006944 days
 - = 6 days + 0,456006944 days \times 24 h
 - = 6 days + 10,94416667 h
- ∴ 10,94416667 h
 - = 10 h + 0,94416667 h
 - = 10 h + 0,94416667 \times 60 min
 - = 10 h + 56,65 min
- ∴ 56,65 min
 - = 56 min + 0,65 min \times 60 s
 - = 56 min + 39 s
- ∴ 557 799 s
 - = 6 days; 10 h; 56 min and 39 s

Let's Practice!

4. The table below shows the running times of two different athletes during the 2015 Comrades Marathon at various points along the route. One of the athletes won the marathon and the other came second.

Athlete A				Athlete B			
Place on the route	te Distance run (km) Total running time (h, min, s)		Place on the route	Distance run (km)	Total running time (h, min, s)		
Lion Park	15,9	01:08:07		Lion Park	15,9	01:05:26	
Camperdown	26,9	01:55:19		Camperdown	26,9	01:50:39	
Halfway	45	03:13:20		Halfway	45	03:05:14	
Pinetown	68,9	05:01:32	1	Pinetown	68,9	04:54:45	
Mayville	82,3	06:03:07		Mayville	82,3	06:02:45	
Finish	89,3	06:36:03		Finish	89,3	06:37:30	

- 4.1 Who out of the two athletes came in first?
- 4.2 How far is it from Pinetown to the Finish?
- 4.3 How long (in hours, minutes and seconds) did it take Athlete A to run from Lion Park to Halfway?
- 4.4 How long (in hours, minutes and seconds) did it take Athlete B to run from Camperdown to Mayville?
- 4.5 Approximately where in the race did Athlete A overtake Athlete B? Explain your answer.

Answers

- 4.1 Runner A
- 4.2 Distance to Pinetown = 68,9 km Distance to Finish = 89,3 km
 - ∴ Distance from Pinetown to Finish
 = 89,3 km 68,9 km
 = 20,4 km
- 4.3 Running time at Lion Park = 1 h 8 min 7 s Running time at Half Way = 3 h 13 min 20 s ∴ 3 h ; 13 min ; 20 s <u>- 1 h ; 8 min ; 7 s</u> 2 h ; 5 min ; 13 s
- 4.4 Running time at Camperdown = 1 h 50 min 39 s Running time Mayville = 6 h 2 min 45 s 5 60 + 2 = 62 min
 - ∴ 6′h ;2′min ;45 s <u>-1 h ;50 min ;39 s</u>
 - 4 h ; 12 min ; 6 s
- 4.5 Between Mayville and the Finish, i.e. Runner B came through Mayville in a quicker time than Runner A,

but Runner A then finished the race before runner B. So Runner A passed Runner B somewhere between Mayville and the Finish.

TIME

Let's Practice!

- 5. Pete is an avid leisure fisherman and keeps an eye on the tide timetable. Study the Simon's Town Tide Timetable for a part of November 2014 below in order to answer the following questions:
- 5.1 Write down the solar times for 3 November in 12-hour format.
- 5.2 Calculate the time difference between the Spring Tide and Lowest Tide on 6 November.
- 5.3 On which days should Pete go out fishing? Give a reason for your answer.
- 5.4 How much later is the first low tide on 4 November, as opposed to the first low tide on 5 November?
- 5.5 Pete is only able to go out fishing on Saturday, 8 November, from 2:15 pm -5:00 pm. What percentage of his fishing time out will be considered as the 'best fishing time?

SIMON'S TOWN TIDE TABLE NOVEMBER 2014

Sunday	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday			
						1			
						SOLAR			
FISH-O-METER									
Best fishing days									
		Good fish	ning days			Moonset 01:58			
		Solupar	Theory			Underfoot 07:42			
		Please note that	the best fishing	1		Moonrise 13:31			
	pe	riods are for the	leisure fisherm	an		TIDE TIMER			
	a	nd peak fishing	times during nig	ht		Low tide 04:00			
		time have no	t been listed.			High tide 10:19			
		Spring	g Tide:			Low tide 17:01			
		06 Nov 2014 @	2 14:43 (1,92 m)			REST EISHING			
		Lowes	t Tide:			DESTINISTING			
Lowest Inde: 06 Nov 2014 @ 21:02 (0,23 m)									
) ²	3	4	05	6	07	E B			
SOLAR	SOLAR	SOLAR	SOLAR	SOLAR	SOLAR	SOLAR			
Sunrise 05:44	Sunrise 05:43	Sunrise 05:42	Sunrise 05:41	Sunrise 05:40	Sunrise 05:40	Sunrise 05:3			
LUNAR	LUNAR	LUNAR	LUNAR	LUNAR	LUNAR	LUNAR			
Moonset 02:39	Moonset 03:19	Moonset 03:58	Moonset 04:38	Moonset 05:19	Overhead 00:33	Overhead 01:2			
Underfoot 08:35	Underfoot 09:27	Underfoot 10:20	Underfoot 11:13	Underfoot 12:06	Moonset 06:03	Moonset 06:5			
Overhead 21:01	Overhead 21:53	Overhead 22:46	Overhead 23:39	Overhead:	Moonrise 20:01	Moonrise 21:0			
TIDE TIMES	TIDE TIMES	TIDE TIMES	TIDE TIMES	TIDE TIMES	TIDE TIMES	TIDE TIMES			
Low tide 05:20	High tide 00:12	High tide 01:04	High tide 01:49	High tide 02:30	High tide 02:30	High tide 03:4			
High tide 11:33	Low tide 06:21 High tide 12:31	Low tide 07:11 High tide 13:19	Low tide 07:55 High tide 14:02	Low tide 08:36 High tide 14:43	Low tide 08:36 High tide 14:43	Low tide 09:5 High tide 15:5			
High tide:	Low tide 18:59	Low tide 19:44	Low tide 20:24	Low tide 21:02	Low tide 21:02	Low tide 22:1			
BEST FISHING	BEST FISHING	BEST FISHING	BEST FISHING	BEST FISHING	BEST FISHING	BEST FISHING			
12:05 to 13:07	13:03 to 14:05	H 13:51 to 14:53	H 14:34 to 15:36	14:11 to 15:15	14:49 to 15:53	14:24 to 15:26			

Answers

5.1 Sunrise (05:43) → 5.43 am Sunset (19:16) \rightarrow 7.16 pm

$20 \quad 60 + 2 = 62$

- Lowest tide: 21:92 5.2 - Spring tide: - 14:43 6:19 .: 6 hours 19 minutes
- 5.3 3 8 November as the 'Fish-O-Meter' indicates these are the 'Best fishing days'.
- 5.4 First low tide on 5 November: 07:55 - First low tide on 4 November: - 07:11 00:44

.:. 44 min later

- 5.5 Fishing Time out:
 - ▶ 2.15 pm 5.00 pm
 - 16 60
 - : 17:90 - 14:15
 - 2:45

▹ Best fishing time: 14:24 - 15:26 .: 15:26 - 14:24

- 1:02 \therefore 1 h 2 min best fishing time
- $\Rightarrow \% = \frac{\text{best fishing time}}{\text{fishing time out}} \times 100\%$ $=\frac{1 h 2 min}{2 h 45 min} \times 100\%$ 1 h 2 min $= \frac{62 \min}{165 \min} \times 100\%$ 2 h 45 min = 37.58%

